## Course Syllabus

## I. General Information

| Course name | Calculus II |
| :--- | :--- |
| Programme | Mathematics |
| Level of studies (BA, BSc, MA, MSc, long-cycle <br> MA) | BA |
| Form of studies (full-time, part-time) | Full-time |
| Discipline | Mathematics |
| Language of instruction | English |


| Course coordinator/person responsible | dr Andrzej Michalski |
| :--- | :--- |


| Type of class (use only <br> the types mentioned <br> below) | Number of teaching <br> hours | Semester | ECTS Points |
| :--- | :--- | :--- | :--- |
| lecture | 60 |  |  |
| tutorial |  |  |  |
| classes | 60 | III |  |
| laboratory classes |  |  |  |
| workshops |  |  |  |
| seminar |  |  |  |
| introductory seminar |  |  |  |
| foreign language <br> classes |  |  |  |
| practical placement |  |  |  |
| field work |  |  |  |
| diploma laboratory |  |  |  |
| translation classes |  |  |  |
| study visit |  |  |  |


| Course pre-requisites | Calculus I |
| :--- | :--- |

## II. Course Objectives

To present the basic concepts and theorems in calculus of several variables.
To develop skills in applied calculus of several variables.

## III. Course learning outcomes with reference to programme learning outcomes

| Symbol | Description of course learning outcome | Reference to programme learning outcome |
| :---: | :---: | :---: |
| KNOWLEDGE |  |  |
| W_01 | Basic concepts and definitions of calculus of several variables (K_W01, K_W02, K_W03, K_W04, K_W05, K_W07). | $\begin{aligned} & \hline \text { K_W01, K_W02, } \\ & \text { K_W03, K_W04, } \\ & \text { K_W05, K_W07 } \\ & \hline \end{aligned}$ |
| W_02 | Basic methods and theorems of calculus of several variables (K_W01, K_W02, K_W03, K_W04, K_W05, K_W07). |  |
| W_03 | Selected applications of calculus of several variables (K_W01, K_W02, K_W03, K_W04, K_W05, K_W07). | $\begin{aligned} & \hline \text { K_W01, K_W02, } \\ & \text { K_W03, K_W04, } \\ & \text { K_W05, K_W07 } \end{aligned}$ |
| SKILLS |  |  |
| U_01 | ```Solve typical problem using standard methods (K_U01, K_U02, K_U03, K_U04, K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, K_U15).``` | $\begin{aligned} & \text { K_U01, K_U02, } \\ & \text { K_U03, K_U04, } \\ & \text { K_U05, K_U06, } \\ & \text { K_U10, K_U12, } \\ & \text { K_U13, K_U14, } \\ & \text { K_U15 } \end{aligned}$ |
| U_02 | Analyze complex problem, propose and explain the optimal methods for its solution (K_U01, K_U02, K_U03, K_U04, K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, K_U15). | $\begin{aligned} & \text { K_U01, K_U02, } \\ & \text { K_U03, K_U04, } \\ & \text { K_U05, K_U06, } \\ & \text { K_U10, K_U12, } \\ & \text { K_U13, K_U14, } \\ & \text { K_U15 } \end{aligned}$ |
| U_03 | Solve selected practical problems (K_U01, K_U02, K_U03, K_U04, K_U05, K_U06, K_U10, K_U12, K_U13, K_U14, K_U15). | $\begin{aligned} & \text { K_U01, K_U02, } \\ & \text { K_U03, K_U04, } \\ & \text { K_U05, K_U06, } \\ & \text { K_U10, K_U12, } \\ & \text { K_U13, K_U14, } \\ & \text { K_U15 } \end{aligned}$ |
| SOCIAL COMPETENCIES |  |  |
| K_01 | Formulate and present opinions on the applicability of calculus methods taking into account own knowledge and skills (K_K01, K_K05). | K_K01, K_K05 |

## IV. Course Content

Continuity and differentiability of functions of several variables. Higher order derivatives. Local and global extreme values. Implicit function. Local invertibility. Extreme values of an implicit function. Lagrange coefficients method. Mappings in Cartesian spaces. Multiple integrals. Iterated integrals. Change of variables. Line integrals. Green's theorem. Surface integrals. Divergence (GaussOstrogradsky) theorem. Stokes theorem. Applications.

| Symbol | Didactic methods <br> (choose from the list) | Forms of assessment <br> (choose from the list) | Documentation type <br> (choose from the list) |
| :--- | :--- | :--- | :--- |
| W_01 | conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
| W_02 | conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
|  | Conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
|  | conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
| U_02 | conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
| U_03 | conventional lecture, <br> discussion, practical <br> classes | test, written exam, oral <br> exam | evaluated test, protocol |
| K_01 | conventional lecture, <br> discussion, practical <br> classes | SOCIAL COMPETENCIES <br> test, written exam, oral <br> exam | evaluated test, protocol |

## VI. Grading criteria, weighting factors.....

LECTURE:
The completion of classes is required. Written and oral exam together constitute the final grade (after each semester):
91-100\% excellent
$81-90 \%$ very good
71 - 80\% good
$61-70 \%$ satisfactory
$51-60 \%$ sufficient
less than 51\% fail
CLASSES:
At least $80 \%$ of attendance is required. Two tests together constitute the final grade (each semester):
91 - 100\% excellent
$81-90 \%$ very good
71 - 80\% good
$61-70 \%$ satisfactory
$51-60 \%$ sufficient
less than 51\% fail

Detailed assessment rules are given during lectures and classes.

## VII. Student workload

| Form of activity | Number of hours |
| :--- | :--- |
| Number of contact hours (with the teacher) | Lecture: 60 hrs. <br> Classes: 60 hrs. <br> Individual consultations: 30 hrs. <br> In total: 150 hrs. |
| Number of hours of individual student work | Preparation for classes: 60 hrs. <br> Studying books: 45 hrs. <br> Preparation for tests and exams: 45 hrs <br> In total: 150 hrs. |

## VIII. Literature

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Basic literature
Lecture notes.
Worksheets.
Additional literature
In English:
R. Ellis, D. Gulick, Calculus: One and Several Variables, Harcourt Brace Jovanovich, }1991
D. D. Berkey, P. Blanchard, Calculus, Saunders College Pub., }1992
S. L. Salas, E. Hille, J. T. Anderson, Calculus: One and Several Variables with Analytic Geometry,
Wiley, 1986.
In Polish:
W. Rudin, Podstawy analizy matematycznej, PWN, Warszawa }2002
M. Gewert, Z. Skoczylas, Analiza Matematyczna 2, Oficyna Wydawnicza GiS, 2005.
M. Gewert, Z. Skoczylas, Elementy analizy wektorowej. Teoria, przykłady, zadania., Oficyna
Wydawnicza GiS, }2012
W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach, PWN, }2004
J. Banaś, S. Wędrychowicz, Zbiór zadań z analizy matematycznej, WNT, Warszawa }1996
G. Fichtenholz, Rachunek różniczkowy i całkowy, PWN, 2005.
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